TRANSIENT COMPACT MODELING FOR MULTI CHIPS COMPONENTS

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ABSTRACT

In this paper, we present a methodology to generate transient 3D Nonlinear Compact Thermal Models (CTMs) for multi-chip electronic components and systems. This method is based on defining the Optimal Thermal Coupling Point (OTCP) that simplifies generating the CTMs. The CTMs are presented by RC network that enables us to make full and fast electro-thermal calculations in one simulation process by using PSpice or any electrical simulation software. This paper is a continuity for research work that aims at reducing the number of RC elements, indeed the proposed work differs from nodal method that induce significant number of RC elements, while remaining faithful to the physical phenomena to model.

1. INTRODUCTION

The goal of finding CTMs is to extract a simple presentation of the thermal behavior without going so far in the complexity of calculations, and without increasing the data that have to be calculated. However, this model has to achieve several important points like:
- A minimum error in comparison with the 3D thermal analyzing software.
- Possibility to adapt any thermal boundary conditions.
- Short calculation time.

In the literature we can find several thermal models that deal with the nonlinearity phenomena or the 3D effects [1] [2] [3], but those which take into account all the phenomena at once are very complex. For circuits and component thermal management, designers need simple and accurate CTMs which are able to achieve realistic electro-thermal simulations. The presented method deals with:
- The problem of multi-chips system and the thermal coupling between them.
- The nonlinear behavior of certain parameters like thermal conductivity of semiconductors.
- The transient thermal response.

In the following, we depict our methodology in successive steps; starting from the simplest problem (single source) to multi-sources generalized problem.

2. STRUCTURE WITH ONE HEATING SOURCE

Figure 1 – Structure of one heating source

The practical work begins by solving the thermal problem, and finding the steady state temperature of all chosen points (central point of each sub-layer). In this step, we use Rebeca-3D®, Flotherm® or any other 3D thermal simulation software. The procedure of calculating the thermal resistances $R_{th,3D}$ begins by calculating the value of $R_{th,3D}$ for each sub-layer by the following formula:

$$R_{th,3D} = \frac{T_i - T_{i-1}}{P} \quad (K^°/W)$$

The second step is achieved by applying the equation that presents the relation between the temperature and the conductivity in the $R_{th,1D}$ formula (in our case only Silicon presents non-linear thermal characteristics).

$$k_{Si}(T) = 154.68\left(\frac{300}{T}\right)^{\frac{4}{3}} \quad (W/m.K^°)$$

$$R_{th,p} = \frac{e_{Si}}{S_{Si}k_{Si}} \quad (K^°/W)$$
From (2) and (3) we get:

$$R_{\text{th},D-\text{nonlinear}} = \frac{e_{\text{Si}}}{S_{\text{Si}} \cdot 1.5468 \frac{300}{T} \frac{1.5468 \frac{300}{T}}{4/3}} = \frac{R_{\text{th},D}}{300 \left( \frac{300}{T} \right)^{4/3}}$$

Then, to transform the 1D non-linear equation to 3D one, we apply a correction coefficient given by the ratio between the $R_{\text{th},1D}$ and $R_{\text{th},3D}$:

$$R_{\text{th},D-\text{nonlinear}} = \frac{R_{\text{th},D}}{300 \left( \frac{300}{T} \right)^{4/3}} \cdot \frac{R_{\text{th},D}}{300 \left( \frac{300}{T} \right)^{4/3}} = \frac{R_{\text{th},D}}{300 \left( \frac{300}{T} \right)^{4/3}}$$

The final step is to introduce equation (5) in the expression of VCC (Voltage Controlled Current) control element, which can be found in ABM library of PSpice[4].

In order to enhance the nonlinearity phenomena by inducing a large temperature shift, we have made a simulation with a 250W of dissipated power and we got the next table of values:

<table>
<thead>
<tr>
<th>Layer</th>
<th>Rebeca-3D nonlinear aspect</th>
<th>1D-$R_{\text{th}}$</th>
<th>Nonlinear 3D-$R_{\text{th}}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Si1</td>
<td>97.571 (°C)</td>
<td>118.675 (°C)</td>
<td>97.701 (°C)</td>
</tr>
<tr>
<td>Si2</td>
<td>89.175</td>
<td>112.275</td>
<td>89.163</td>
</tr>
<tr>
<td>Si3</td>
<td>81.129</td>
<td>105.875</td>
<td>81.015</td>
</tr>
<tr>
<td>Cu1</td>
<td>73.369</td>
<td>99.475</td>
<td>73.174</td>
</tr>
<tr>
<td>Cu2</td>
<td>52.694</td>
<td>74.65</td>
<td>52.624</td>
</tr>
<tr>
<td>Cu3</td>
<td>37.486</td>
<td>49.825</td>
<td>37.475</td>
</tr>
</tbody>
</table>

Table 1: Extracted temperatures by Rebeca-3D, compared with ones obtained by 1D and 3D-nonlinear CTMs.

3. STRUCTURE WITH TWO HEATING SOURCES

When we apply a power on the first source, we can see that the generated isothermal surfaces take nearly the shape of half-sphere, one of them presents the temperature of the second source, which is inactive, and by applying the power on the second source we get the same effect (see Fig.2).

The intersection between these two half-sphere is an arc that each point of it can present the thermal coupling between the two sources. The simplest is to choose the point that locates at the vertical central axis between the two sources; this point is the Optimal Thermal Coupling Point (OTCP).

To illustrate in a practical example, we take the structure which is presented in fig.3, all this structure is made of Silicon in order to highlight the nonlinear properties of thermal conductivity.

By applying the power on one of the two sources and launching the thermal simulation process with Rebeca-3D, we get the temperature of the points (A, B, C, and D). Because of the symmetry of structure, we can say that the value of thermal resistances between (A and B), (B and E) are the same as thermal resistances between (D and C), (C and E).

To calculate these thermal resistances we use the same formula as in the case of single source (1), so we get:

$$R_{3D_{A-B}} = \frac{R_{3D_{C-E}}}{20} = \frac{50.35 - 25.433}{20} = 0.488 \text{ (K}/\text{W})$$

$$R_{3D_{D-E}} = \frac{R_{3D_{C-E}}}{20} = \frac{25.433 - 25}{20} = 0.02165 \text{ (K}/\text{W})$$

Finally, we apply the equation (5) in the expression of PSpice element (VCC). Fig.5 presents the corresponding CTM drawn in PSpice simulation software.
To validate our method, we launch a thermal simulation process by using Rebeca-3D with the nonlinearity aspect and dissipate a power of 40W on the first source and 50W on the second one, at the same time we launch the thermal simulation process on our compact model using P-Spice. Table 2 presents the temperature for each point (A, B, C, and D) obtained from Rebeca-3d with nonlinear aspect, the 3D CTM, and the 3D-Nonlinear CTM.

<table>
<thead>
<tr>
<th>Point</th>
<th>Rebeca-3D</th>
<th>3D-Nonlinear</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>139.722(°C)</td>
<td>142.27(°C)</td>
</tr>
<tr>
<td>B</td>
<td>100.508</td>
<td>105.765</td>
</tr>
<tr>
<td>C</td>
<td>84.019</td>
<td>86.799</td>
</tr>
<tr>
<td>D</td>
<td>113.138</td>
<td>113.517</td>
</tr>
</tbody>
</table>

Table 2 –comparison between Rebeca-3D nonlinear aspect and CTM after improvement

So we launch the thermal simulation three times (because the asymmetrical structure), for each simulation, only one source dissipates 40W (fig. 7). So we obtain from Rebeca-3D the temperature of each source listed in table 3:

<table>
<thead>
<tr>
<th>Point</th>
<th>Power on Source1</th>
<th>Power on Source2</th>
<th>Power on Source3</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>101.346(°C)</td>
<td>25.538(°C)</td>
<td>25.375(°C)</td>
</tr>
<tr>
<td>B</td>
<td>25.538</td>
<td>101.346</td>
<td>29.359</td>
</tr>
<tr>
<td>C</td>
<td>25.375</td>
<td>29.359</td>
<td>101.344</td>
</tr>
</tbody>
</table>

Table 3–The temperature of each point by Rebeca-3D

When we draw our model in p-Spice, we observe several important points:

1 - Because of the current of the sources 1, 2 and 3 are divided into two branches (see fig. 7 and 8), the value of calculated $R_{th-3D}$ have to be multiplied by (n-1) where n is the number of the sources.

2 - The calculations of the thermal resistances assume that: by applying a power on source 1, the temperature of X1 is the same as B, and X2 is the same as C and so on (see fig. 7). But in the electrical presentation of our CTM this principal is not valid because there is a current flow in the resistances R2, R4, R5 and R6 when we apply the power on source 1 (see fig. 8-a), so treating each two sources separately is not possible. To solve this problem, we add on each branch an ideal diode (fig. 8-b) and so we can assure that the calculations of thermal resistances are valid for the electrical representation.
To validate what is explained above, we launch thermal simulation with Rebeca-3D, taking into account the non-linear aspect. We apply on the first source 30W, on the second 40W, and on the third one 20W.

By applying the same dissipated power on our CTM and by dividing the resistances R1, R2, R3, R4, R5, and R6 successively into three resistances (to improve the model) we get the following table which presents the temperature of each source and the points A, B and C, obtained from Rebeca-3D and our 3D-Nonlinear CTM.

<table>
<thead>
<tr>
<th>Point</th>
<th>Rebeca-3D</th>
<th>CTM</th>
</tr>
</thead>
<tbody>
<tr>
<td>Source 1</td>
<td>92.145°C</td>
<td>93.687°C</td>
</tr>
<tr>
<td>A</td>
<td>86.176</td>
<td>87.701</td>
</tr>
<tr>
<td>Source 2</td>
<td>121.317</td>
<td>123.546</td>
</tr>
<tr>
<td>B</td>
<td>112.543</td>
<td>114.685</td>
</tr>
<tr>
<td>Source 3</td>
<td>72.719</td>
<td>70.58</td>
</tr>
<tr>
<td>C</td>
<td>69.002</td>
<td>66.921</td>
</tr>
</tbody>
</table>

Table 4 – The comparison between Rebeca-3D nonlinear aspect and our 3D-Nonlinear CTM.

5. OPTIMIZING THE THERMAL CAPACITANCES

The optimization is based on the physical behavior that can be explained by:

- In the presented CTM (fig.9) we can say, with an accepted accuracy, that the only responsible capacitance for the curve changes of the transient response of junction until the temperature $T_1=P.R_1$ is $C_1$, and for the changes until $T_2=P.(R_1+R_2)$ are both $C_1$ and $C_2$, and so on... (where $P$ is the dissipated power).

- To make the optimization we have to begin by optimizing the value of $C_1$ then $C_2$ and so until the last thermal capacitance.

The benefits of the physical based optimization of the thermal capacitances are summarized by:

1- We are not forced to trace the transient response of several points; just the transient response of the junction is needed.

2- In the case of Multi chips model, it is difficult (practically) to find the physical localization of the thermal coupling points, and this method keep the physical presentation without going in the geometrical calculations.

3- The calculated capacitances are based on the values of the 3D thermal resistances, so they present 3D thermal capacitances.
Figure 11- The flowchart of the thermal capacitances optimization

6. REFERENCES


