Parallelization of a 3-D SPH code for massive HPC simulations

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Abstract:
Smoothed Particle Hydrodynamics (SPH) is a particle method that experienced a large growth in the last two decades. While it was initially developed for astrophysics, today this method is applied to fluid, structures and other complex multiphysics simulations. The SPH-flow code developed jointly by Ecole Centrale de Nantes and HydroOcean is mainly designed to model complex free surface problems in a context of high dynamic phenomena, together with the presence of complex solid geometries interacting with the fluid. In this field, the main advantage of the SPH method relies on its ability to simulate disconnection and reconnection of the free surface without having to capture it. As for other particle methods, this method is demanding in terms of computational resources, and its parallelization is compulsory for large 3-D applications, in order to maintain some reasonable restitution times. The order of magnitude of the resolution involved in our simulations is several hundred million particles, implying the need for thousands of CPU cores. This paper deals with introducing a parallelization strategy based on a domain decomposition within a purely MPI-based distributed memory framework. The results are discussed through a scalability study involving up to 32,768 processors in a network.

Mots clefs : SPH ; HPC ; MPI
1 Introduction

The objective of the present work is to improve the performance of the HPC code SPH-flow developed jointly by Ecole Centrale de Nantes and HydrOcean, to make it efficient in research as well as in industrial contexts. Various problems can be solved using this 2-D/3-D parallel SPH code, such as multifuid flows \cite{4}, Fluid-Structure Interaction (FSI) \cite{3}, and viscous flows \cite{5}. The main difficulties of a SPH model parallelization arise from the interpolation process, based on a kernel function and using possibly variable compact supports. In Section 2, the SPH method is described, together with its kernel-based interpolation feature. In Section 3, the main aspects of the parallelisation performed are introduced. In Section 4, parallel performances are presented and discussed. Finally, industrial test cases involving massively parallel SPH simulations are presented in Section 5.

2 SPH method

The equations to be solved in our field of application are the Euler equations, as classically used to model non viscous fluid flows. One of the main SPH features consists in considering any fluid flow as compressible, resulting in the use of an equation of state to close the system. SPH uses a set of interpolating points (particles) which are initially distributed in the fluid medium. The spatial derivatives present in the Euler equations are then simply interpolated by introducing a kernel function $W$ that is convoluted with the discrete values of the field, as in the following example for the pressure gradient:

$$< \nabla P(\vec{x}) > = \sum_{i=1}^{N} P(\vec{x}_{i}) \nabla W(\vec{x} - \vec{x}_{i}, R) \omega_{i}, \quad (1)$$

where $i$ refers to the particles in the vicinity of location $\vec{x}$ and located within the radius $R$ of the compact support of $W$. Note that this kernel function $W$ implies the same algorithmic needs as the Van der Waals function used in molecular dynamics, requiring the creation of a neighbor list and the computation of particle-to-particle interactions. The main difference resides in the fact that $W$ acts as an actual interpolation function, similarly to the test functions used in Finite Element methods for instance. In their discrete form, the Euler equations become finally

$$\frac{d\vec{x}_{i}}{dt} = \vec{v}_{i}, \quad (2)$$

$$\frac{d\rho_{i}}{dt} = \sum_{j=1}^{N} m_{j} (\vec{v}_{i} - \vec{v}_{j}) \nabla W(\vec{r}_{i} - \vec{r}_{j}, R), \quad (3)$$

$$\frac{d\vec{v}_{i}}{dt} = -\sum_{j=1}^{N} m_{j} \left( \frac{P_{i}}{\rho_{i}^{2}} + \frac{P_{j}}{\rho_{j}^{2}} \right) \nabla W(\vec{r}_{i} - \vec{r}_{j}, R) + \vec{g}, \quad (4)$$

Note that the above scheme corresponds to one of the various examples of SPH formulations available in the literature. As stated in equation (2), each particle moves according to the computed fluid velocity, emphasizing the Lagrangian feature of SPH. Moreover, each of the above derivatives are advanced in time using an explicit time integration scheme such as Runge-Kutta, preventing from the need of any linear system resolution. This explicit and Lagrangian features of SPH stand for the main properties that impact the parallelization of this method. Furthermore, in practice at least $N = 20$ and $N = 70$ neighbors are needed in 2-D and 3-D respectively for the interpolation of each particle $i$, so that the main computational costs rely in the computation of the flux terms of equations (3) and (4).
3 Parallel flux computations and time advance

The parallelization performed here is based on a domain decomposition strategy, which consists in splitting the whole particle domain into sub-domains, and to attribute each sub-domain to each process. The whole domain is therefore "retrieved" through point-to-point MPI communications between processors. In [6], we presented parallel results of computations on up to 2,000 processors. The results were encouraging but exhibited a breakdown, revealing that the communications were not fully overlapped by the computation of the flux terms and/or the time advance. In order to overcome this problem, an overlapped zone is identified. For a given process of interest, this zone is made of three particle groups: the outer particles which are received from the neighbor processes, the inner particles which are sent to the neighbor processes, and the local particles which are neither outer nor inner particles. Local particles are usually more numerous than inner particles. The strategy retained here thus consists in overlapping the communication times of inner particles with the computation times of local particle flux loops. The main difficulty then resides in the creation of such a Local-Inner-Outer zone, which is not straightforward due to the need for an easy identification of the outer particles in the context of variable kernel radii discretisation. To avoid huge communications of particles that do not interact with inner particles, the shape of the overlapped zone must be built piecewise. Finally, time integration of ODEs (3) and (4) can be summarized as in equation (5):

$$\phi_i^{n+1} = \phi_i^n + \delta t \sum_j F_{ij} \quad \forall i \text{ particles}, \quad (5)$$

where $\phi_i^n$ is the variables at time $t_n$ of particle $i$, and $F_{ij}$ the flux between particles $i$ and $j$. The parallel scheme is evaluated as described in Algorithm 1. This scheme ensures that a high parallelisation efficiency can be reached provided that the computational cost of the local particle interaction loops is greater than the communication time of the inner particles.

**Algorithm 1** LIO scheme with communication overlapping.

**Require:** the state variables $\phi_i^n$ on the local, inner and outer particles should be first correctly addressed for all processes.

1: post the MPI reception of the newly updated state variables $\phi_i^{n+1}$ of outer particles.
2: for all interaction of the inner particles with their local, inner and outer neighbor particles do
3: compute the flux terms $F_{ij}$
4: end for
5: for all inner particles $i$ do
6: update $\phi_i^{n+1}$ as in equation (5).
7: end for
8: MPI send of the newly computed state variables of inner particles to neighbor processes
9: for all interactions of the local particles with their local neighbor particles do
10: compute the flux terms $F_{ij}$
11: end for
12: for all local particles $i$ do
13: update $\phi_i^{n+1}$ as in equation (5).
14: end for
15: wait the communication ending of the outer particle state variables.

4 Scalability study in massive HPC context

To study the parallel performances of the two approaches combined, two distinct studies can be performed. The first one consider a fixed problem size while the number of processes increases. Ideally the reduction factor of the CPU time on $p$ processes should be $\frac{1}{p}$, but we generally introduce the speedup which is the inverse of this factor. Such a study is called "strong scalability" study, and is presented in Subsection 4.1. Another study may consider a fixed problem size per process. In this case, the communications increase as the number of processes increase. This study named "weak scalability"
study enables to identify some MPI communications bottlenecks. The results are exposed in Subsection 4.2. The study presented hereafter have been performed on the facilities provided by CSCS. The code has been executed on Monte Rosa, fitted with AMD Interlagos 2 x 16-core 64-bit CPUs, 32 GB per compute node and high performance networking with Gemini 3D torus interconnect. It features a total of 1,496 nodes, corresponding to 47,872 cores, with a theoretical peak performance of 402 TFlops.

4.1 Strong scalability

Figure 1 shows the results obtained for a total of $10^7$ particles from 8 to 256 cores, for $10^8$ particles from 256 to 16,384 cores and $10^9$ particles from 4,096 to 32,768 cores.

Figure 1 shows that the code scales linearly but with a slope that remains lower than the ideal speedup. Due to the nature of our implementation, the boundaries are taken into account with some specific treatments, which implies that some extra interactions must be computed. These treatments suffer from some defects in terms of parallelization. As a result, as the proportion of near-boundary particles decreases while the number of particles increases, this defect tends to present a lower relative importance for very large simulations. For $10^8$ particles, the speedup tends to start saturating from 16,384 processors. For the simulation involving 1 billion particles, a linear speedup is obtained, even when 32,768 cores are used.

4.2 Weak scalability

The weak scalability study is a way to define as how the time to solution varies with the number of processors for a fixed problem size per processor. Note that a fixed number of numerical time steps is applied for each case.

Figure 2 shows that the efficiency obtained is nearby 95%. There is no performance decrease, showing that the communications are therefore fully overlapped by the computations.

Monte Rosa is fitted with 32 cores per node. As a result, in order to avoid bus bandwidth bottlenecks, the weak scalability is started from a reference of 32 processors. Figure 2 shows that the efficiency obtained is nearly 95%. There is no performance decrease, showing that the communications are therefore fully overlapped by the computations.
5 Industrial test cases

Two distinct applications of the SPH-flow code are presented in this part with the improvements described above. These 3-D applications require a large number of points and therefore an efficient HPC code.

5.1 Sphere impact

This test case consists of the 3-D impact of a sphere at the free surface. The sphere of radius $R = 1\text{m}$ is moving at a constant imposed vertical velocity $U = -1\text{m/s}$. The slamming coefficient is defined as $C_S = \frac{F_z}{\frac{1}{2}\rho U^2 \pi R^2}$. A convergence study is performed here for three different resolutions. The particle sizes in the impact area for the different meshes are $2 \times 10^{-2}m$, $1 \times 10^{-2}m$ and $5 \times 10^{-3}m$.

<table>
<thead>
<tr>
<th>$\Delta x$ (m)</th>
<th>N particles</th>
<th>N CPU</th>
<th>CPU time (h)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$2 \times 10^{-2}$</td>
<td>$1 \times 10^6$</td>
<td>32</td>
<td>3.2</td>
</tr>
<tr>
<td>$1 \times 10^{-2}$</td>
<td>$4.4 \times 10^6$</td>
<td>64</td>
<td>15.1</td>
</tr>
<tr>
<td>$5 \times 10^{-3}$</td>
<td>$24.1 \times 10^6$</td>
<td>256</td>
<td>45</td>
</tr>
</tbody>
</table>

Table 1 – CPU datas of the sphere impact.

A snapshot of the free surface deformations is given in figure 3, and CPU data are summarized in table 1. Figure 3 shows that the results obtained converge towards the solution given by Baldwin & Steves [1] and Battistin & Iafrati [2].

![Figure 3](image)

**Figure 3** – Left : snapshot of the sphere impact simulation involving 25 millions of particles. Right : convergence study related to the sphere impact.

5.2 Lifeboat water entry

This case consists in the free fall of a lifeboat in calm water. A correct assessment of loads and slamming pressures on a lifeboat during its entry in the sea is essential for both structural and human safety. The present simulation has been performed for three resolutions : 1, 10 and 100 millions of particles. CPU data are summarized in table 2.

<table>
<thead>
<tr>
<th>N particles</th>
<th>N CPU</th>
<th>CPU time (h)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$1 \times 10^6$</td>
<td>64</td>
<td>3</td>
</tr>
<tr>
<td>$10 \times 10^6$</td>
<td>512</td>
<td>5</td>
</tr>
<tr>
<td>$100 \times 10^6$</td>
<td>2048</td>
<td>30</td>
</tr>
</tbody>
</table>

Table 2 – CPU datas of the lifeboat free fall.
Figure 4 shows the comparison for the three resolutions. As expected, the free surface jets created by the lifeboat water entry are captured more and more accurately.

6 Conclusion

A strategy to carry out 2-D and 3-D massively parallel SPH simulations has been presented. This has been achieved by introducing a domain decomposition framework with effective non-blocking communications. Very good scalability has been obtained for billion particle problems on several thousands of processors. In order to further improve the parallel performances, a particular attention should be paid to the implementation. All the duplicated instructions between processes should be avoided, especially the boundary handling. A future way to reduce the simulation run-times would be to combine our approach with GPGPU approaches, in order to handle flux computations on graphic processors.

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Références

[1] L. Baldwin, H.X. Steves Vertical water entry of spheres, NSWC/WOL/TR 75-49, White Oax Laboratory, Silver Spring, MD, USA, 1975